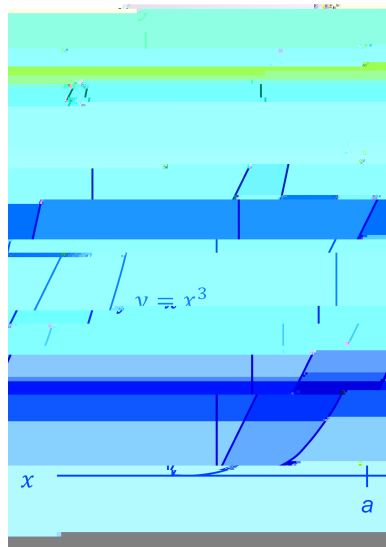


1. (10 points) Solve the following initial value problem:

$$\frac{dy}{dx} = x^2 \csc(y); \quad y(2) = 0:$$

Write your answer in the form $y = f(x)$.

2. (12 pts) Consider the lamina depicted below, which is bounded above by a line through the origin and below by the curve $y = x^3$ on the interval $0 \leq x \leq a$. The line and the curve intersect at $x = 0$ and at $x = a$. The lamina has a uniform density of ρ . What value of a is needed so that $x = 1$?



3. (28 pts) Consider the region R , in quadrant I, bounded by the x -axis, the y -axis, $y = 2$, and $y = \ln(2x)$.
- Use the grid below to sketch and shade the region R . Label the coordinates of the intersections of two curves. (You may find it helpful to know that $e^2 \approx 7.4$.)
 - Set up but do not evaluate expressions involving integrals to determine each of the following:
 - The volume of revolution found by revolving the given region about the y -axis using cylindrical shells.
 - The area of the surface generated by rotating the curve $f(x) = \ln(2x)$ with $0 \leq y \leq 2$ about the y -axis.
 - The perimeter of R . (That is, find the arc length of the entire perimeter of R .)
4. (27 pts) Determine if each of the following converges or diverges. Be sure to fully justify your answers using the teeter of \int_R

$$(c) \sum_{n=2}^{\infty} \ln \frac{n^2 + n}{4(9n + 5n^2)}$$

5.